

**SCI-328 Symposium**  
**Flight Testing of Unmanned Aerial Systems (UAS)**  
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**Analysis of the longitudinal stability of a bioinspired morphing UAV**

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**SPAIN**



- 1.0 INTRODUCTION**
- 2.0 LONGITUDINAL STABILITY ANALYSIS**
- 3.0 FLIGHT CONTROL SYSTEM**
- 4.0 REDESIGN OF THE FLIGHT CONTROL SYSTEM**
- 5.0 CONCLUSIONS**

## 1.0 INTRODUCTION

The National Institute for Aerospace Technology (INTA) is developing Bioinspired Unmanned Aerial Vehicles (UAVs).

### Wing-grid model



Winglets at the tip of the wing to simulate the primary feathers of birds.

### Morphing model



Adaptative wing geometry by using Macro Fiber Composite (MFC) actuators.

## 1.0 INTRODUCTION

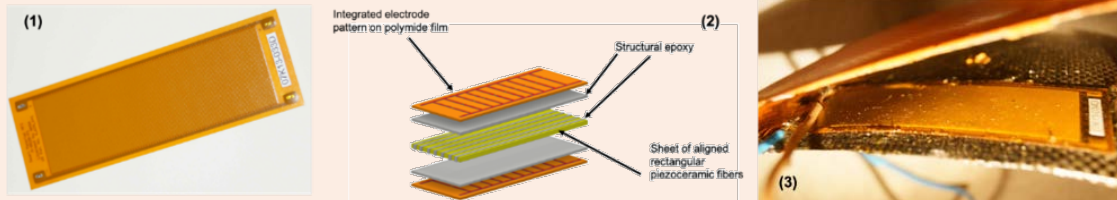
### Morphing Configuration.

Bioinspired morphing UAV

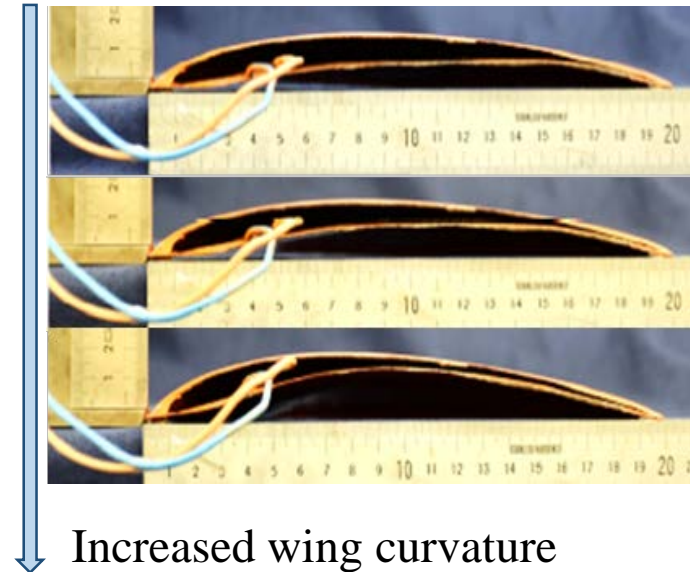


- **Morphing concept:** can be defined as the ability of an aircraft to adapt the geometry of its wings to each flight condition by optimizing the aerodynamic performance in each of them.

Piezoelectric actuators (MFC – Macro Fiber Composite) in the inner part of the wing to modify the curvature.



Some aspects of MFC. (1) M-8528-P1 actuator manufactured by Smart Material Corp selected; (2) MFC structure; (3) Detail of MFC installation over inner part of the wing.



Airfoil curvature with 500 V. No deformation.

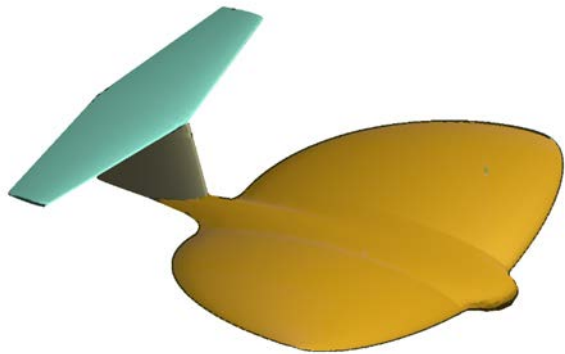
Airfoil curvature with 1000 V.

Airfoil curvature with 1500 V. Maximum deformation.

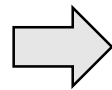
Increased wing curvature

# 1.0 INTRODUCTION

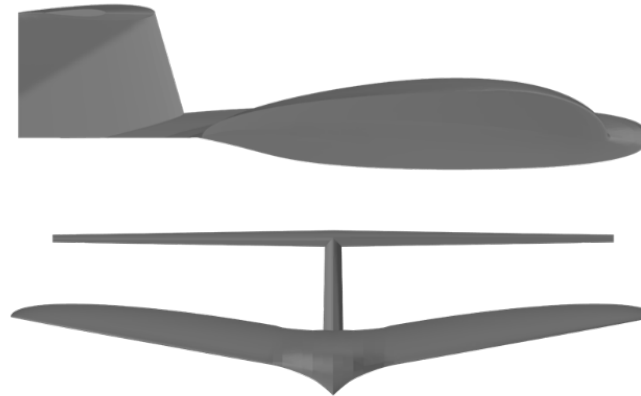
## Bioinspired morphing UAV



- T-tail
- Zimmerman wing
- Wingspan of 320 mm
- Length of 300 mm

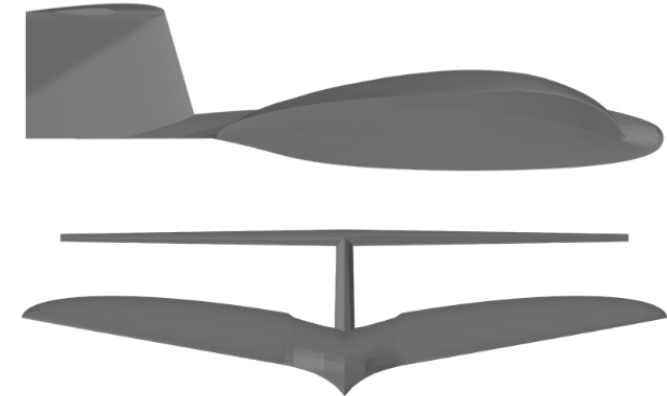


## Base configuration



No wing deformation

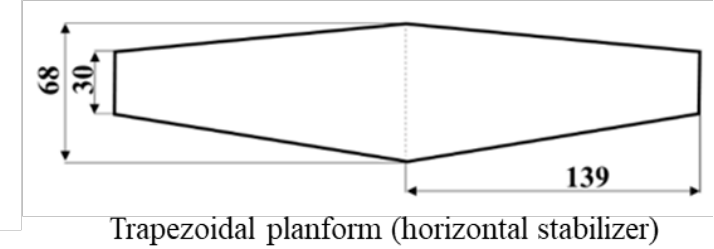
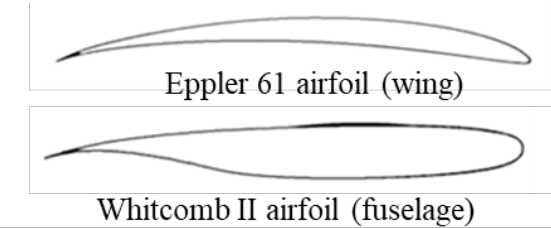
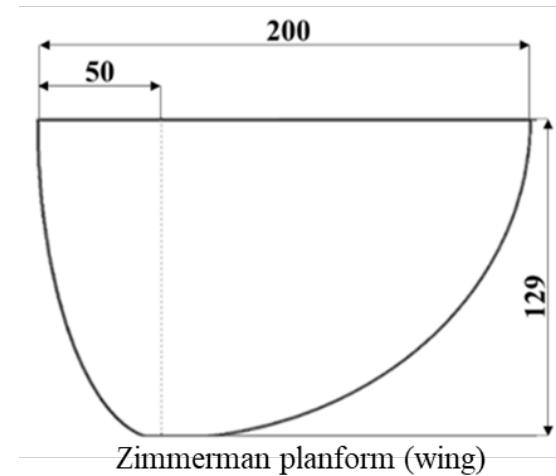
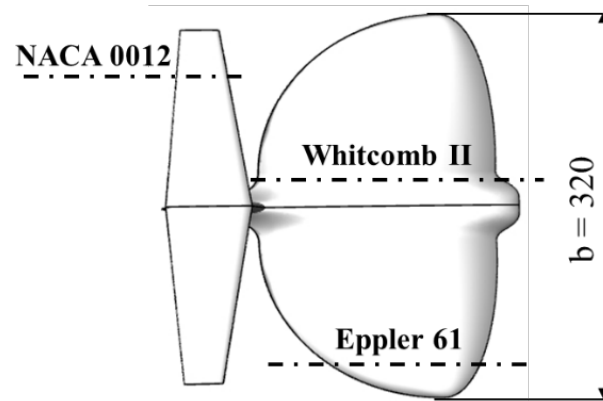
## Modified configuration



Maximum wing deformation

## 1.0 INTRODUCTION

### Geometry.

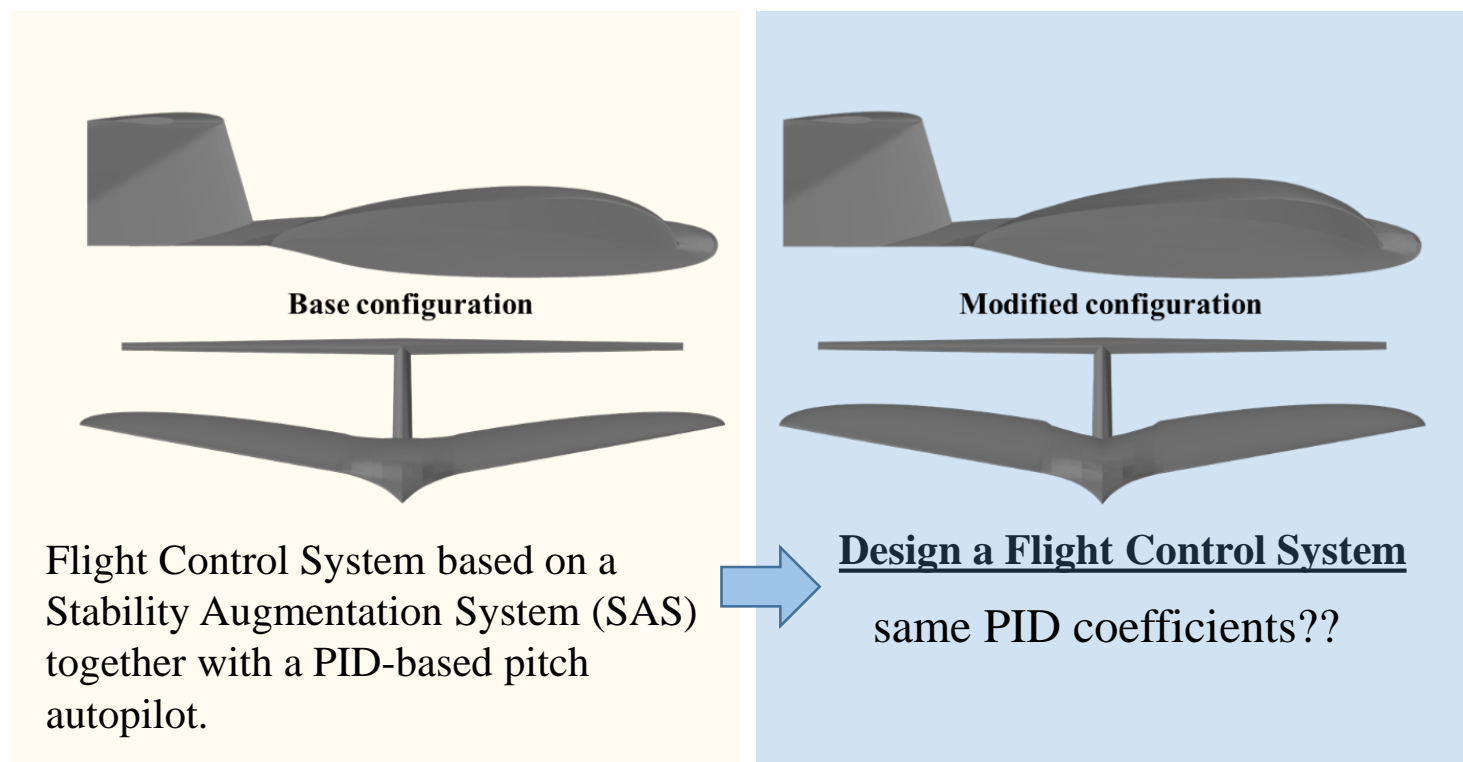


- Zimmerman wing (Eppler 61).
- T-tail (NACA 0012).
- Fuselage (Whitcomb II)

Geometrical Features	Value	Geometrical Features	Value
Reference wing surface, $S_{ref}$	40.000 mm <sup>2</sup>	Mean aerodynamic chord, MAC	141 mm
Fuselage length, $l$	300 mm	Mean geometry chord, MGC	127 mm
Fuselage width, $d$	60 mm	Taper ratio, $\lambda$	0.124
Wingspan, $b$	320 mm	Aspect ratio, $AR$	2.500
Wing tip chord, $c_t$	25 mm	Dihedral angle, $D_h$	10°

## 1.0 INTRODUCTION

- ❑ **Objective:** Redesign the **Flight Control System** for the modified configuration to **improve the dynamic response** of the UAV.





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- 2.0 LONGITUDINAL STABILITY ANALYSIS**
- 3.0 FLIGHT CONTROL SYSTEM**
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## 2.0 LONGITUDINAL STABILITY ANALYSIS

### Longitudinal stability analysis of the base and modified UAV configuration.

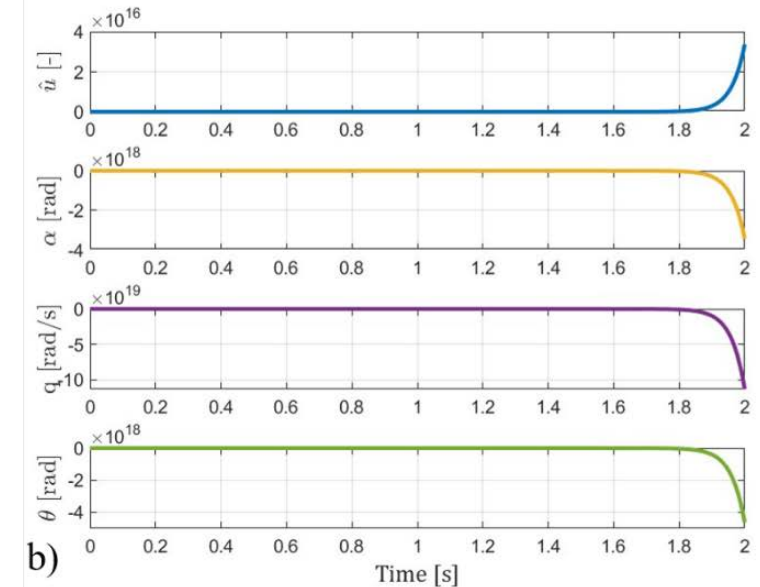
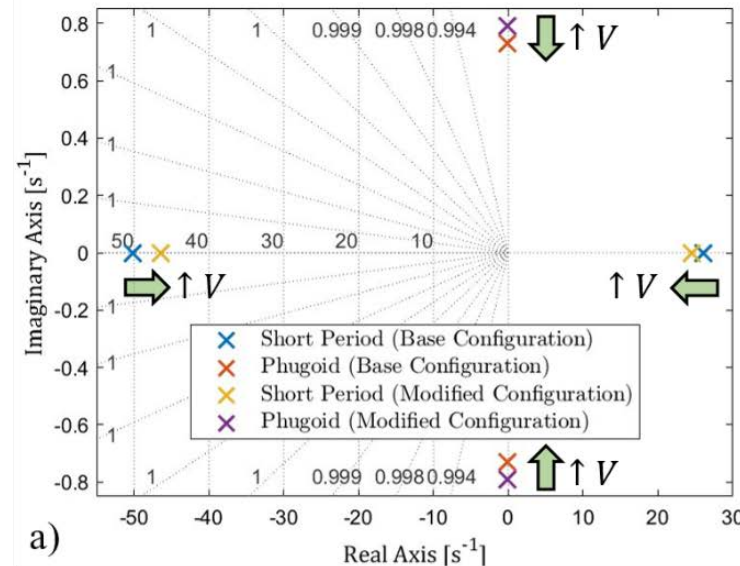
$$c_{m_\alpha} = \frac{\partial c_m}{\partial \alpha} = c_{L_\alpha} (\hat{x}_{cg} - \hat{x}_{ac})$$

$c_{m_\alpha} < 0$ : Statically stable  
 $c_{m_\alpha} > 0$ : Statically unstable

XFLR5 software

$$c_{m_\alpha}^{modified} = 0.67567 \text{ rad}^{-1} > 0$$

$$c_{m_\alpha}^{base} = 0.65744 \text{ rad}^{-1} > 0$$



$\hat{u}$ : non-dimensional velocity.  
 $\alpha$ : angle of attack.  
 $q$ : pitch rate.  
 $\theta$ : pitch angle.

**Statically unstable both UAV configurations !**

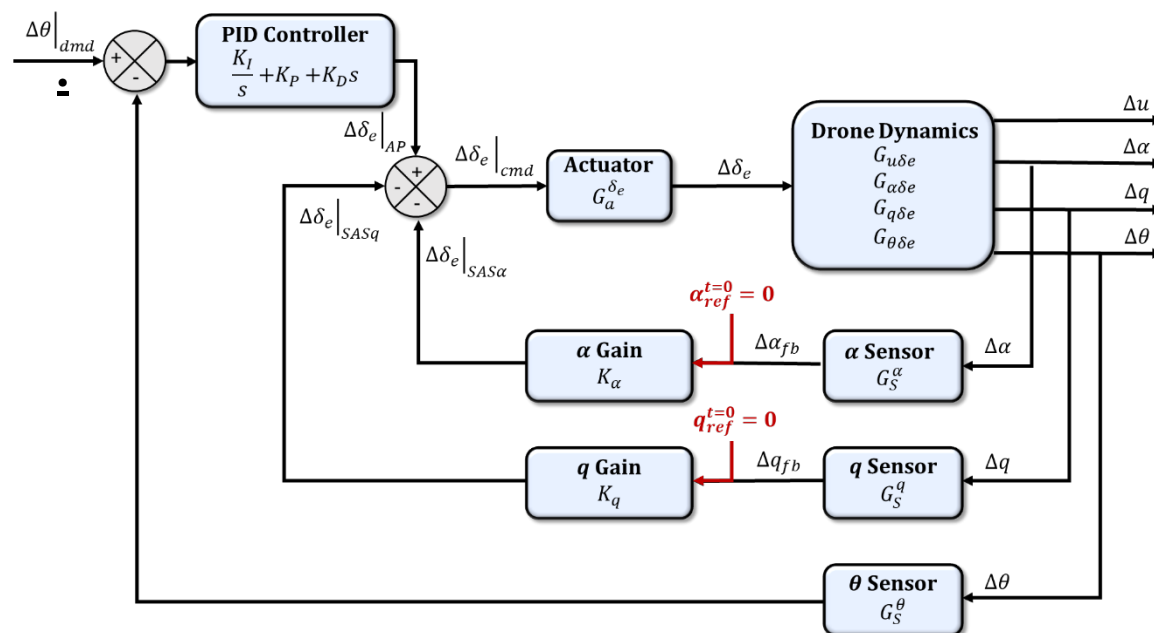


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## 3.0 FLIGHT CONTROL SYSTEM

### Flight control system for the base configuration.

Diagram of the PID-based pitch angle autopilot with an integrated stability augmentation system.



The sensors and actuator involved in the flight control system were modeled as second order transfer functions:

$$G_a^{\delta e} = \frac{w_a^2}{s^2 + 2\xi_a w_a s + 2w_a^2}$$

Characteristic frequency of the actuator,  $w_a = 1/\tau_a$   
 Response delay,  $\tau_a = 0.01$  s  
 Damping coefficient,  $\xi_a = 0.8$

$$G_s = \frac{s^2 - 2w_s s + 2w_s^2}{s^2 + 2w_s s + 2w_s^2}$$

Characteristic frequency of the actuator,  $w_s = 2/\tau_s$   
 Response delay,  $\tau_s = 0.005$  s

$K_\alpha$	$K_q$	$K_P$	$K_I$	$K_D$
-1.375	-0.05	-0.15	-0.18	-0.004

**Statically stable the base configuration !**

## 3.0 FLIGHT CONTROL SYSTEM

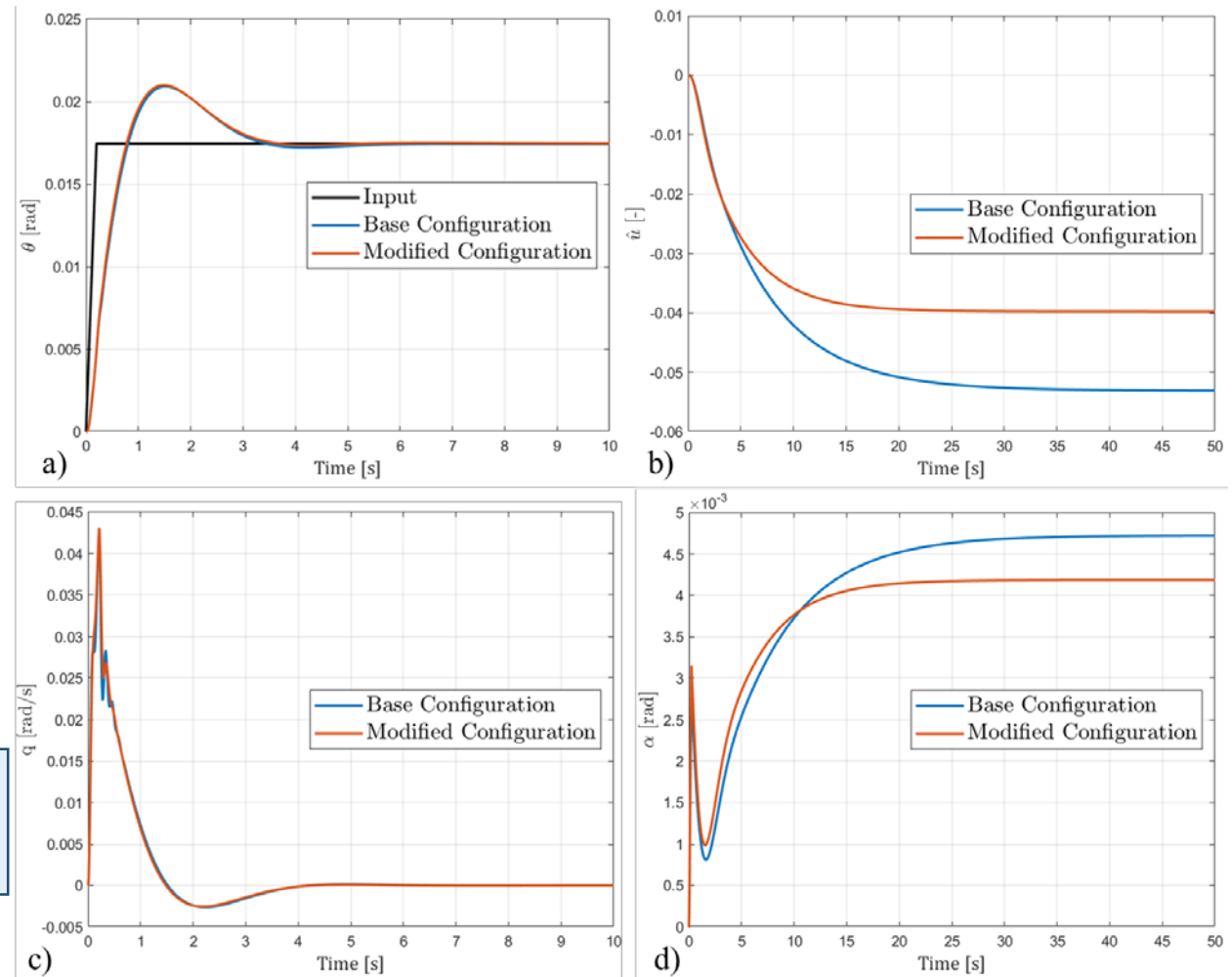
❑ Same gains for both UAV configurations.

❑ Perturbation of the elevator deflection:

1. The non-dimensional velocity  $\hat{u}$  and angle of attack  $\alpha$  time responses differ significantly. Due to the geometrical change.
2. The pitch angle  $\theta$  and pitch rate  $q$  time responses remains the same in both configurations.



**Redesign the Flight Control System Gains for the modified UAV configuration.**

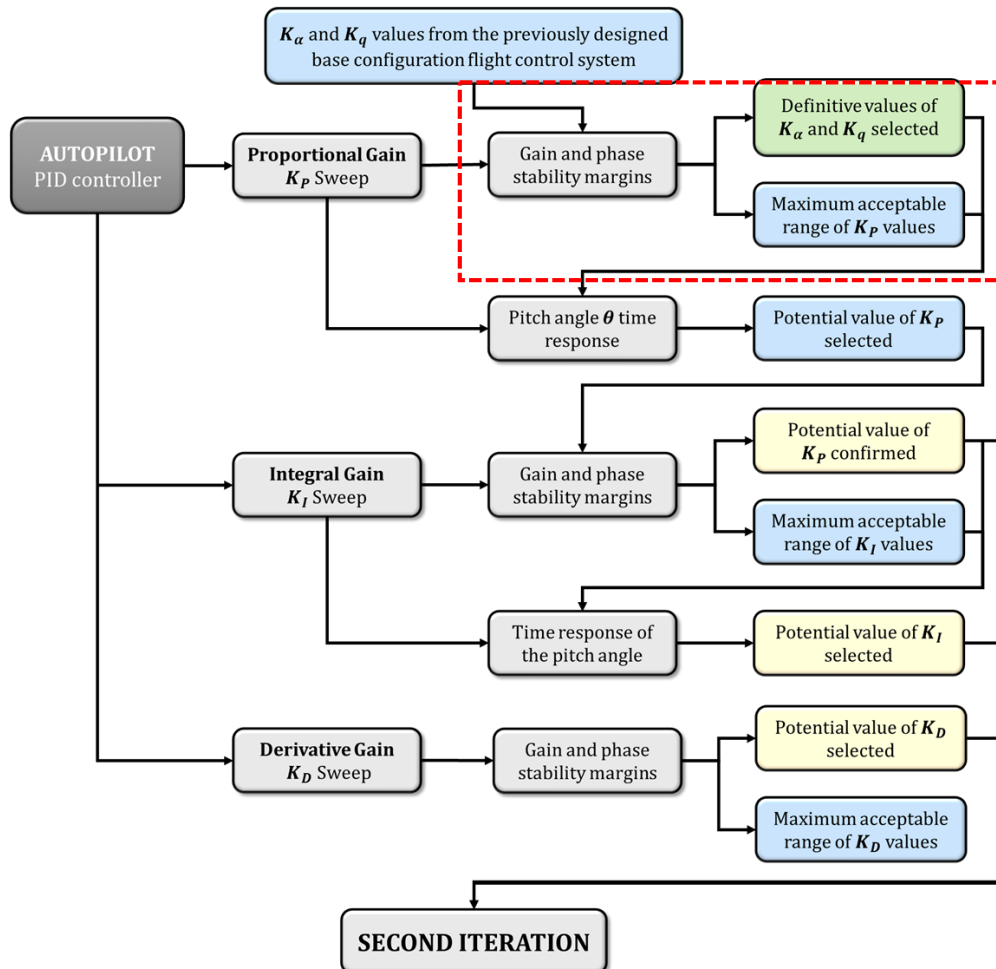




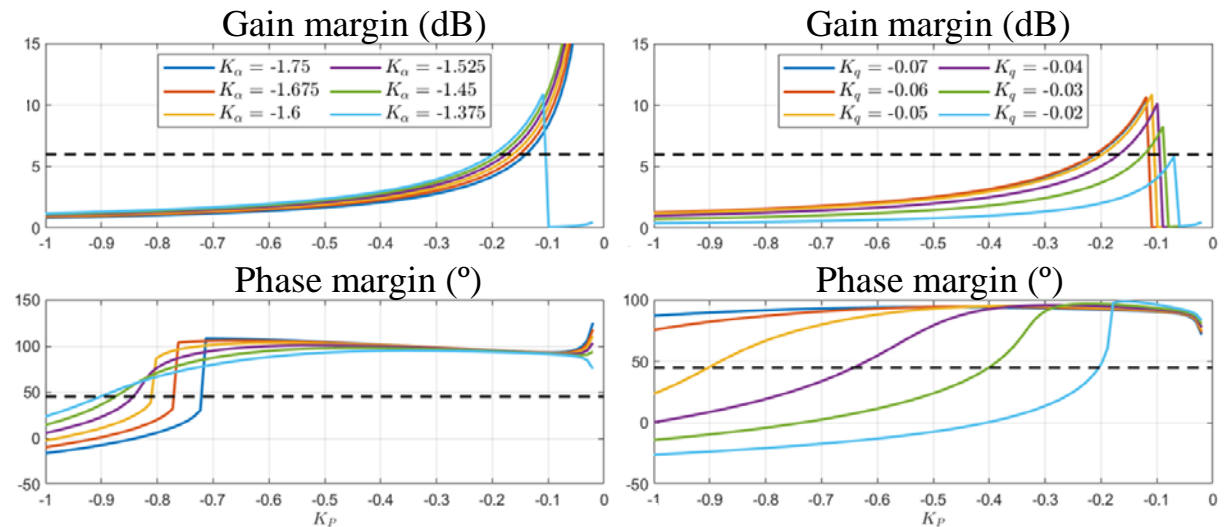
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## 4.0 REDESIGN OF THE FLIGHT CONTROL SYSTEM

**Criteria:**  $GM_{\min} = 6 \text{ dB}$  and  $PM_{\min} = 45^\circ$ .



### Selection of $K_\alpha$ and $K_q$ gains



### Gains obtained for the base UAV configuration

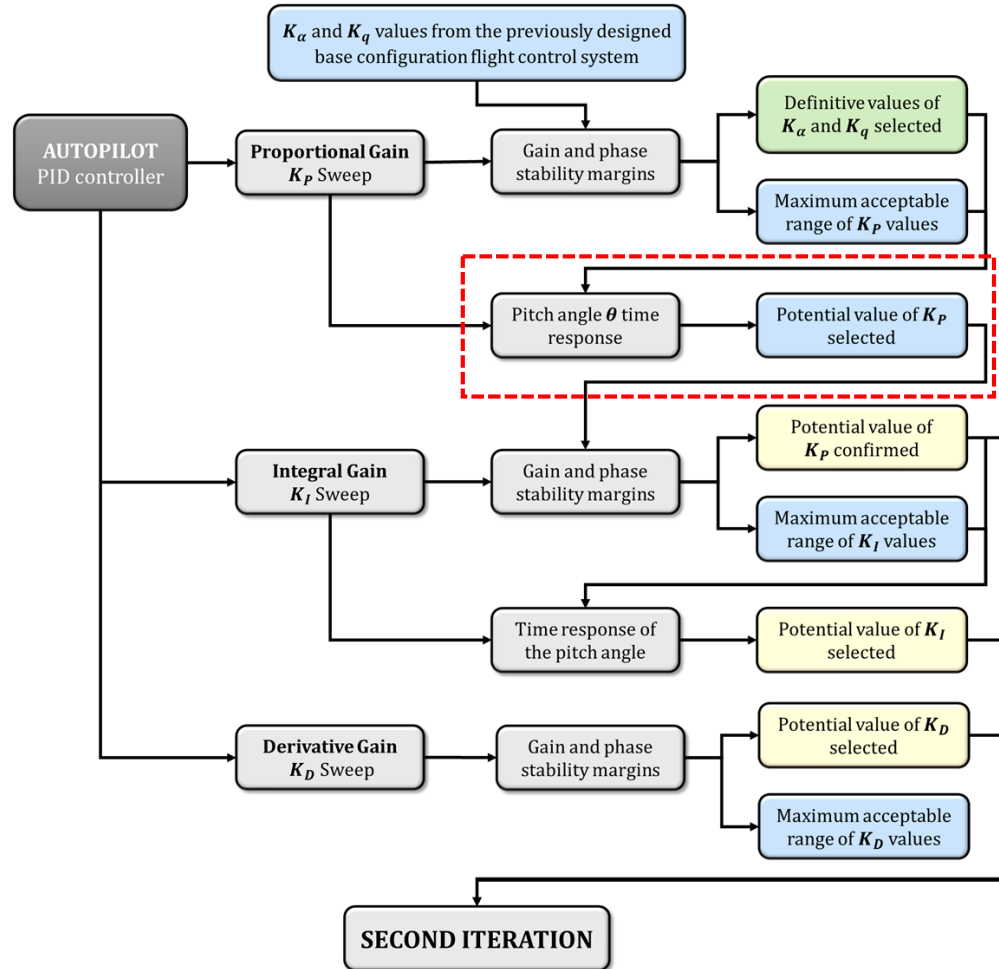
$K_\alpha$	$K_q$	$K_P$	$K_I$	$K_D$
-1.375	-0.05	-0.15	-0.18	-0.004



### Gains obtained for the modified UAV configuration

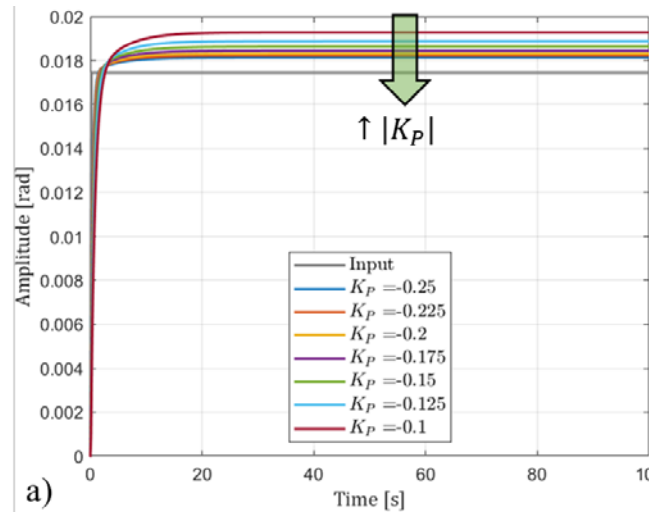
$K_\alpha = -1.375 ; K_q = -0.06$

## 4.0 REDESIGN OF THE FLIGHT CONTROL SYSTEM

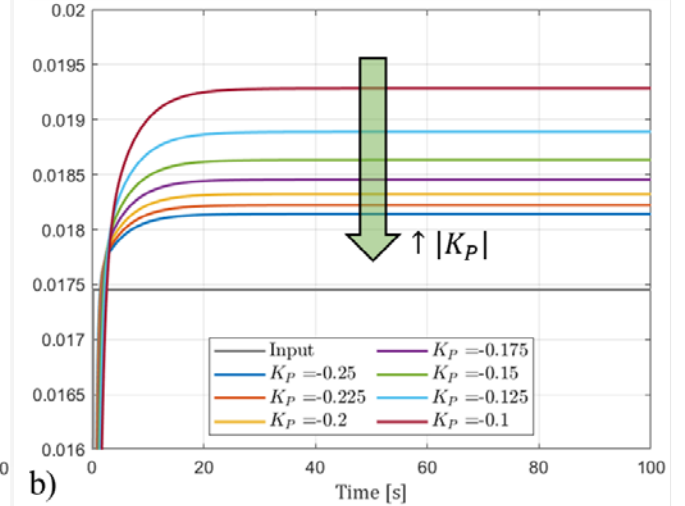


$$K_\alpha = -1.375 ; K_q = -0.06$$

### Selection of $K_p$



### Pitch angle temporal response

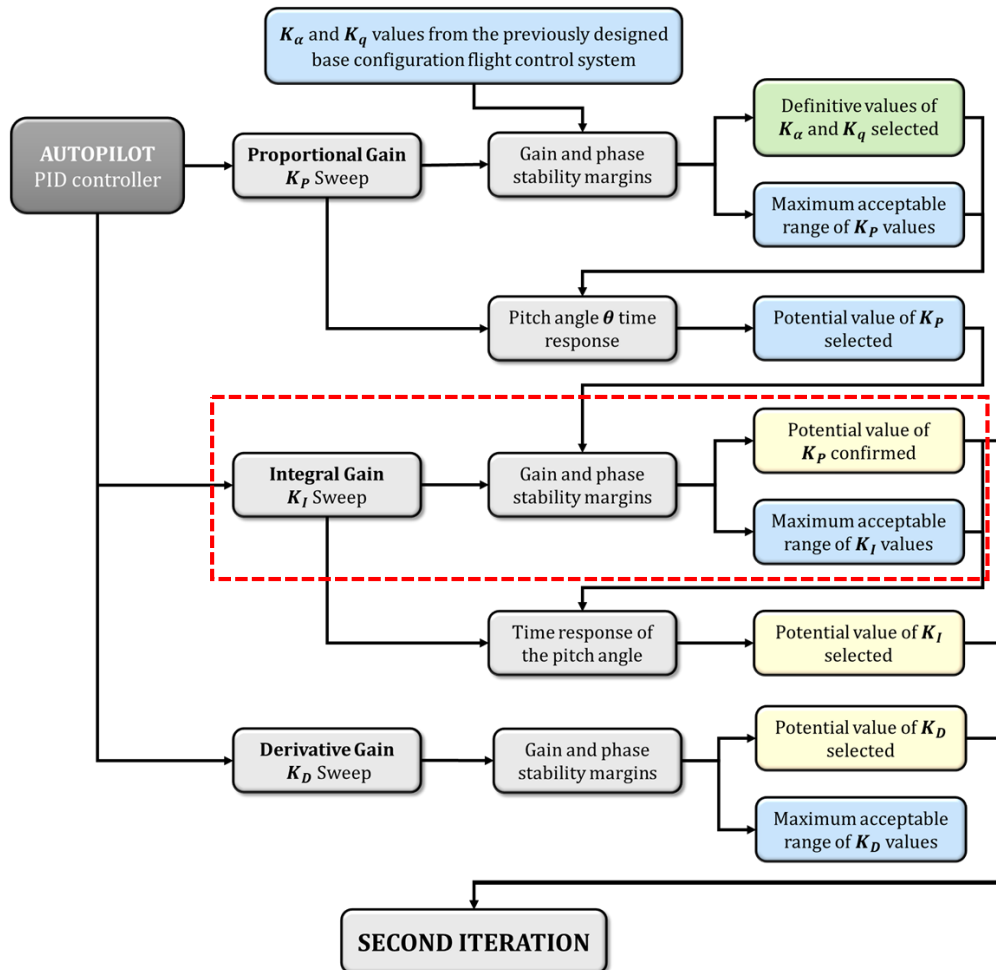


- ↑  $|K_p|$  would be desirable because:
  - The stationary error is reduced.
  - The rise time is slightly reduced.
  - The system response is improved.

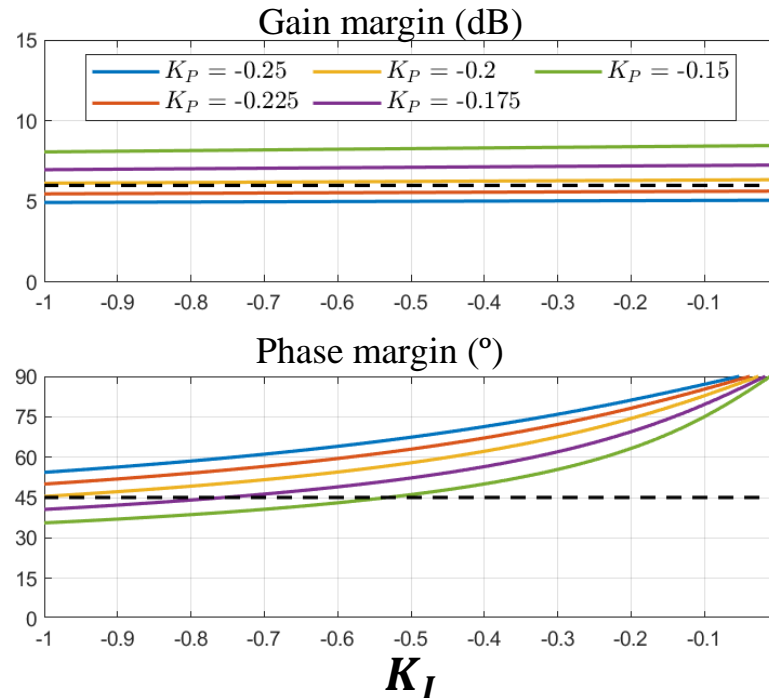


## 4.0 REDESIGN OF THE FLIGHT CONTROL SYSTEM

$K_\alpha = -1.375 ; K_q = -0.06$



### Selection of $K_p$



- Gain margin remains constant for  $K_p$ .
- An increase in  $|K_p|$  benefits the phase margin, but negatively affects the gain margin.



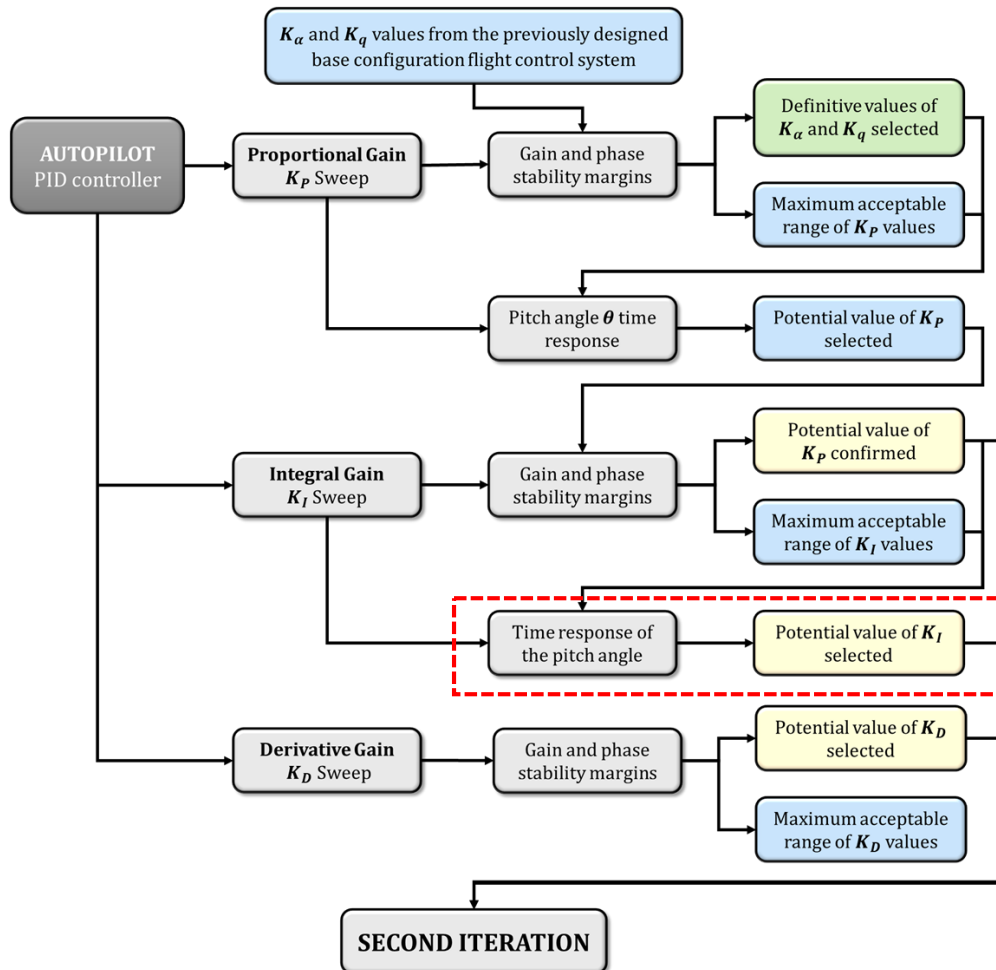
$K_p = -0.2$

- Any value of  $K_I$  could be chosen between -1 and 0.

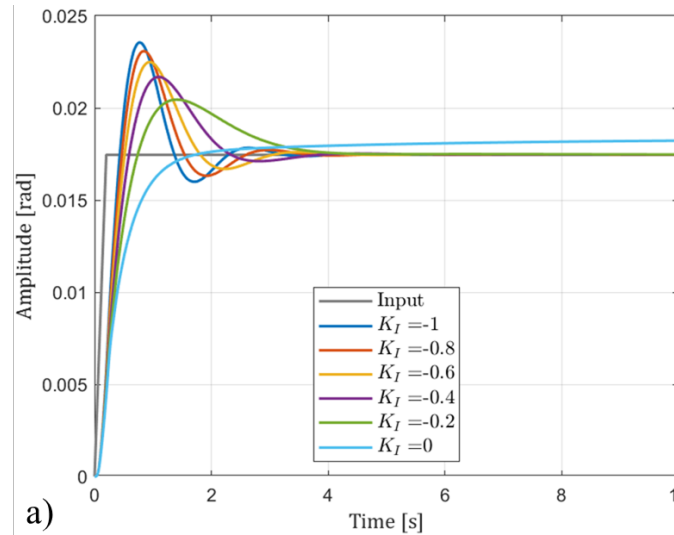


## 4.0 REDESIGN OF THE FLIGHT CONTROL SYSTEM

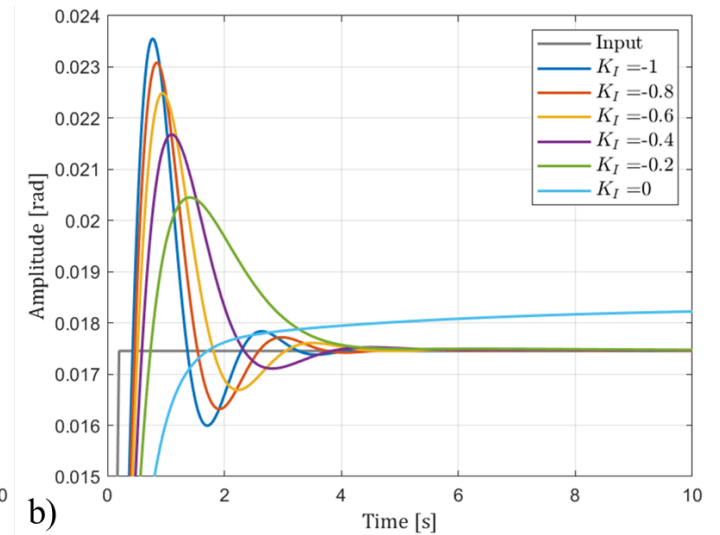
$$K_\alpha = -1.375; K_q = -0.06; K_p = -0.2$$



### Selection of $K_I$



### Pitch angle temporal response



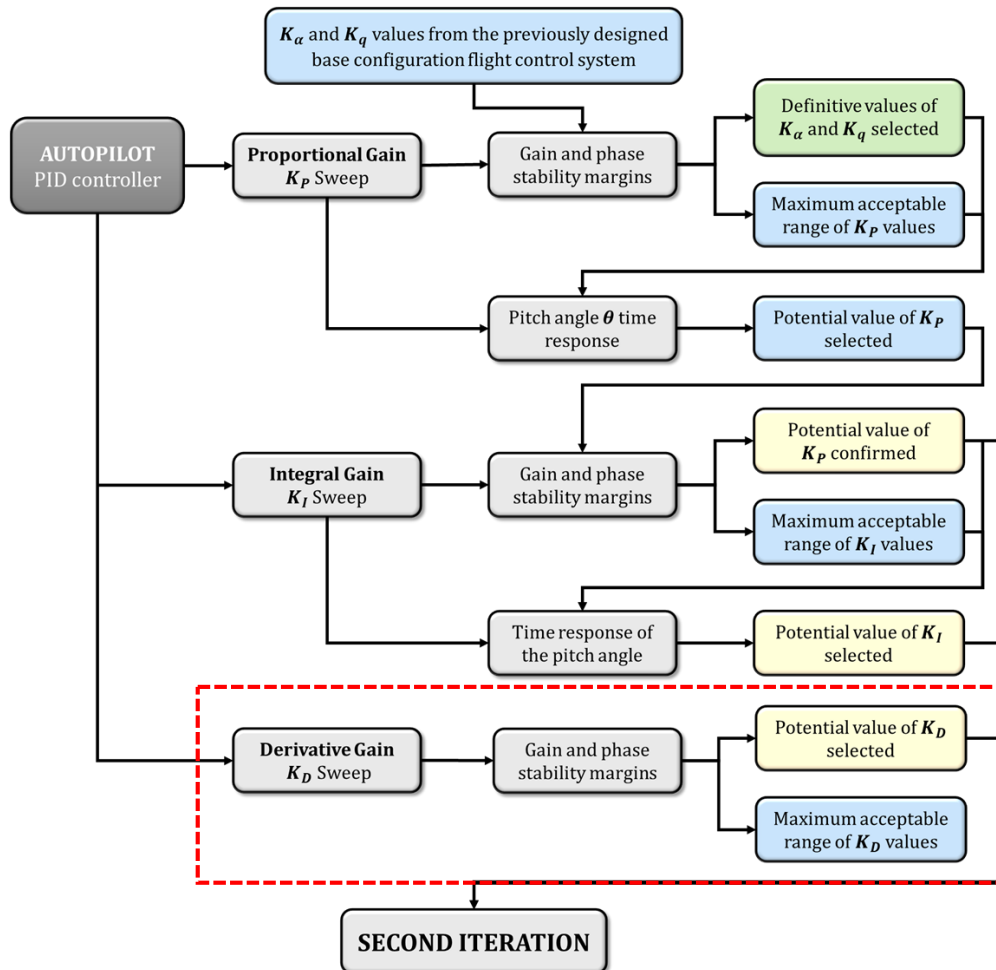
□ ↑  $|K_I|$  :

- the settling time is reduced.
- the response becomes under-damped.
- the overshoot significantly increases.

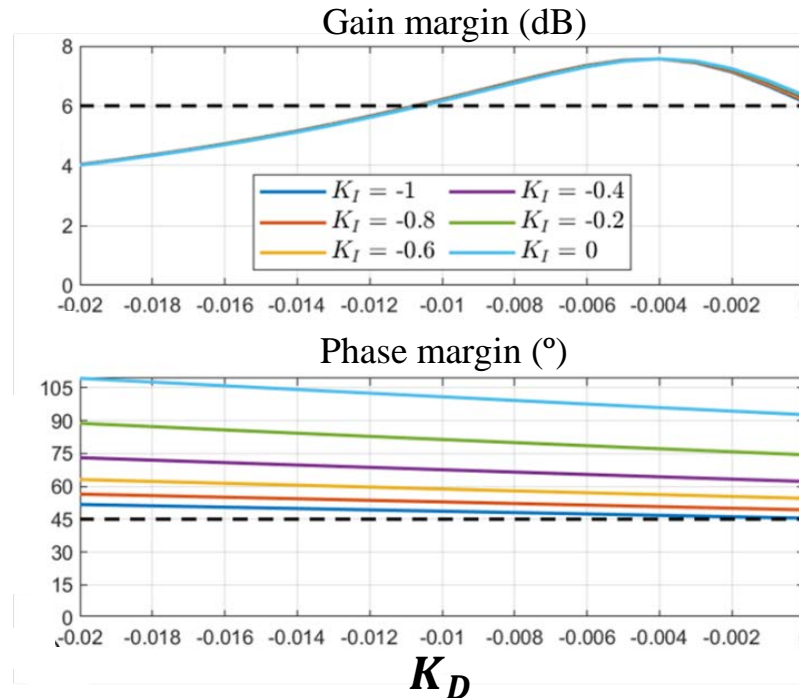


$$K_I \approx -0.5$$

## 4.0 REDESIGN OF THE FLIGHT CONTROL SYSTEM



### Selection of $K_I$



**Very small values of  $K_D$  (-0.01 to 0):**

Any value of  $K_I$  meets the margin and phase margins.



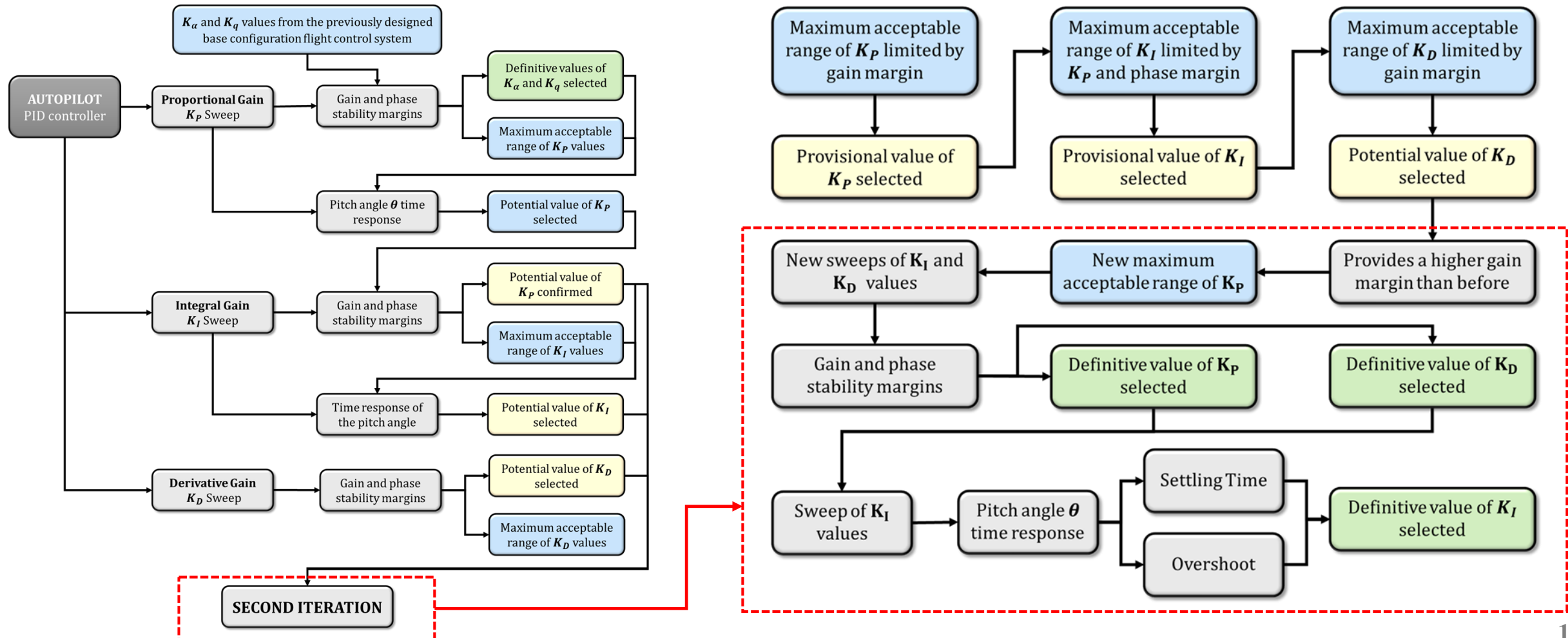
$K_I \approx -0.5$



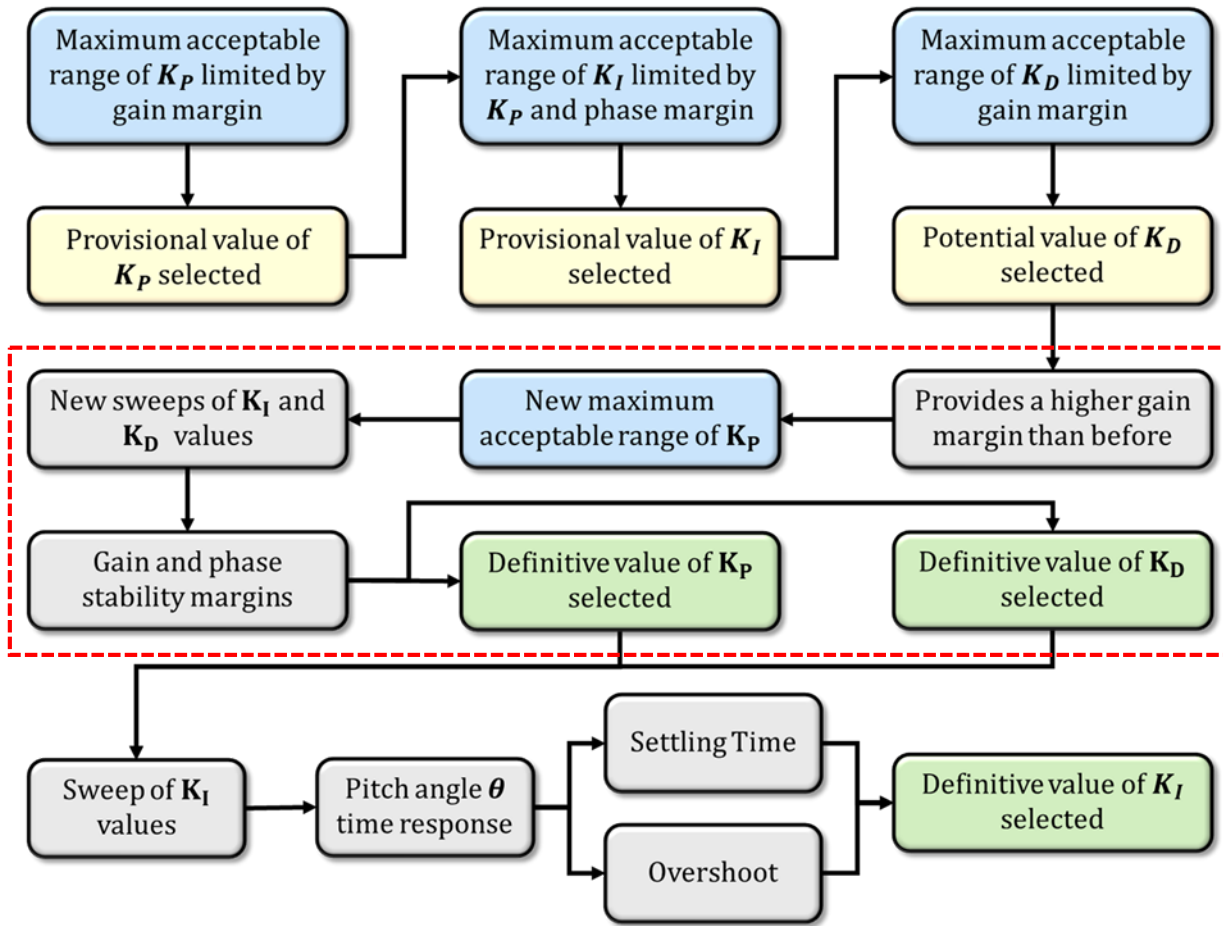
□ Gain margin goes from about 6 dB to almost 8 dB ( $K_D \approx -0.004$ )

$K_p$  can be increased

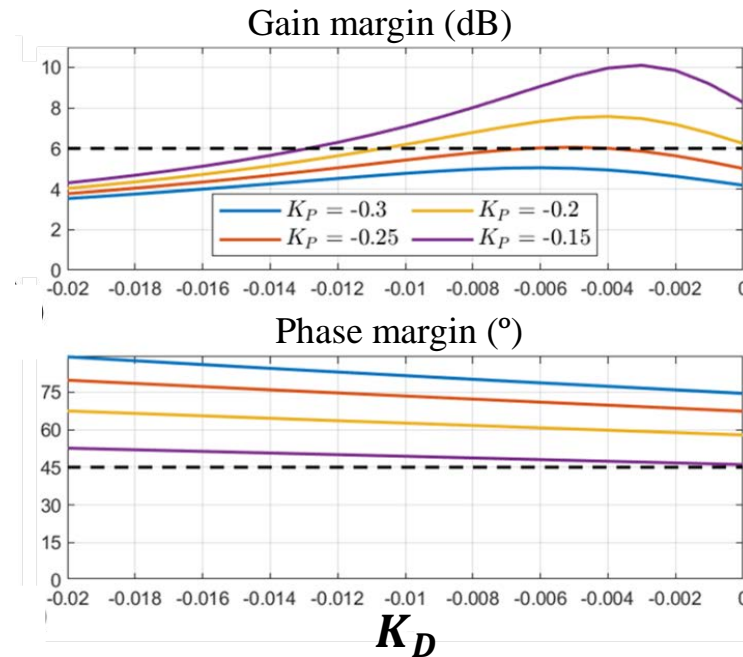
## 4.0 REDESIGN OF THE FLIGHT CONTROL SYSTEM



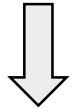
## 4.0 REDESIGN OF THE FLIGHT CONTROL SYSTEM



### Selection of $K_p$ , $K_D$ , $K_I$



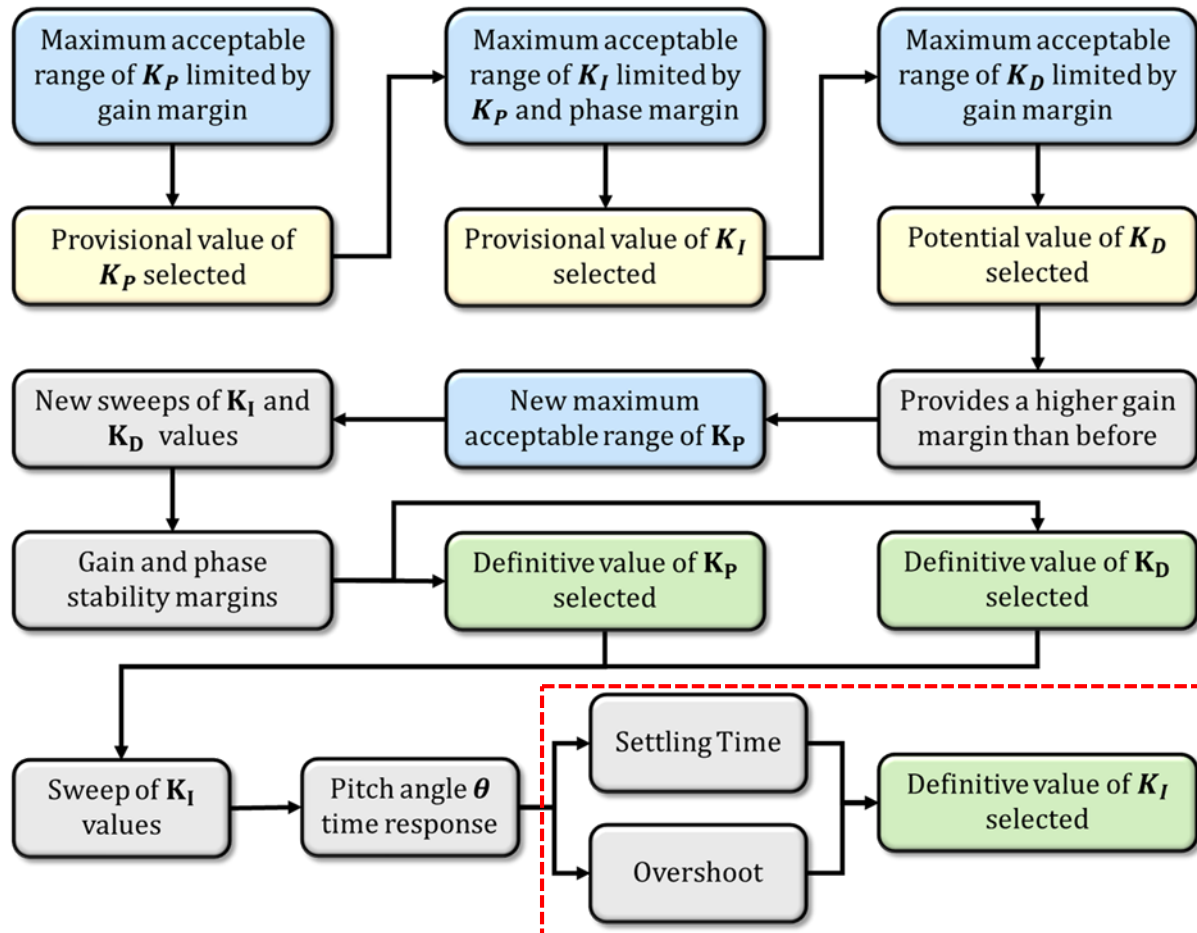
$K_I = -1$



Final gain values

$K_p = -0.25$   
 $K_D = -0.005$

## 4.0 REDESIGN OF THE FLIGHT CONTROL SYSTEM

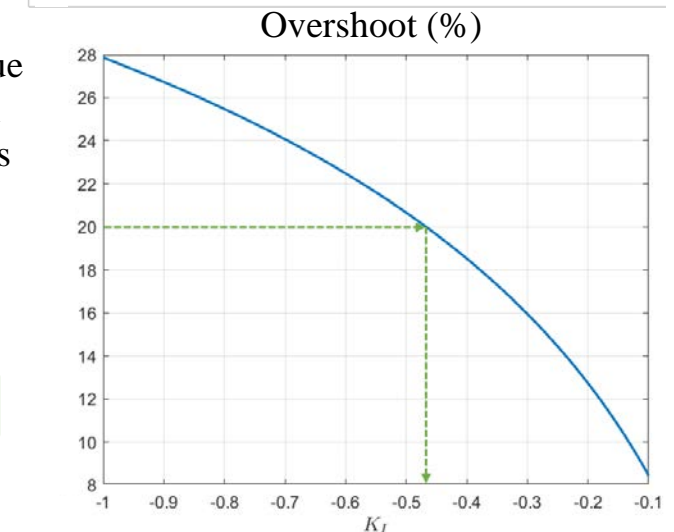
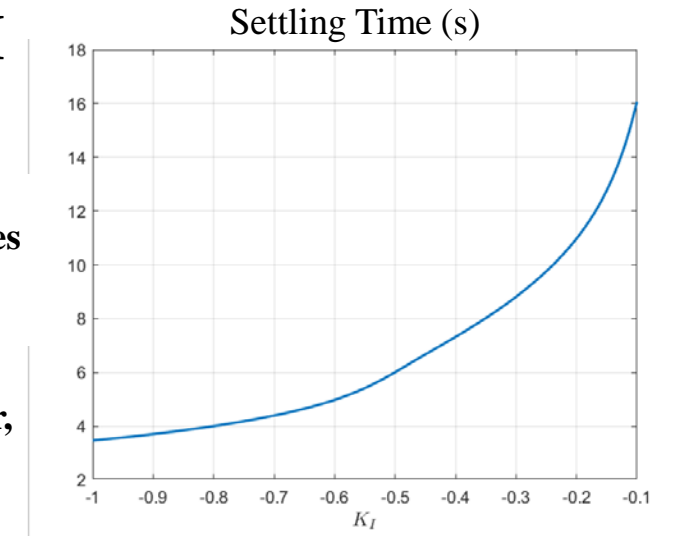


According to Cook in reference “Cook, M., Flight dynamic principles A Linear Systems Approach to aircraft stability and control, Amsterdam etc: Elsevier, 2007.”

an overshoot lower than 20% of the stationary value is mandatory for a control system to be considered as adequate.

Final gain value

$K_I = -0.46$



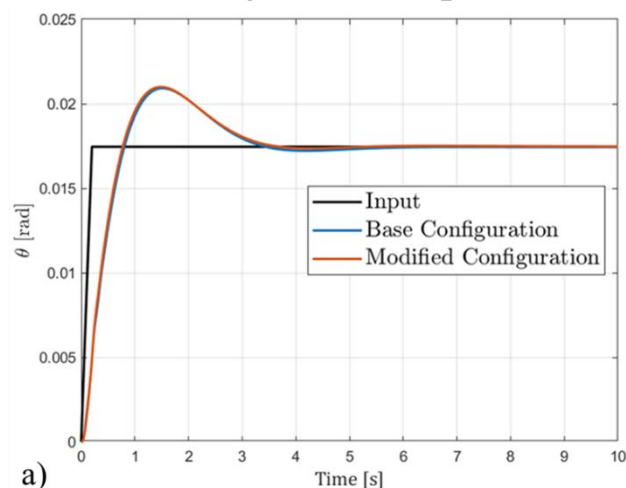


## 4.0 REDESIGN OF THE FLIGHT CONTROL SYSTEM

Final gains of the redesigned flight control system →

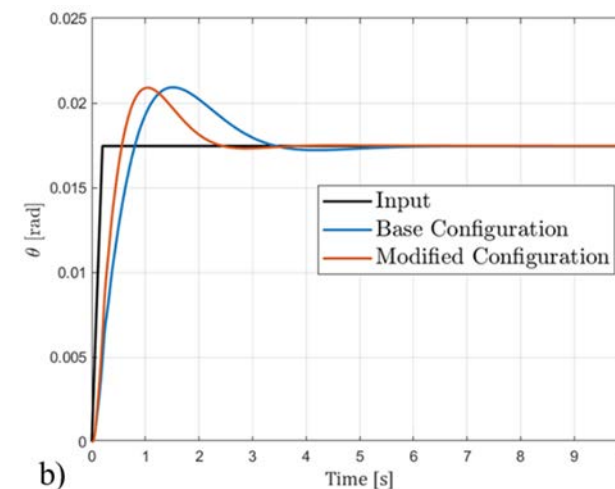
	$K_\alpha$	$K_q$	$K_P$	$K_I$	$K_D$
<b>Base Configuration</b>	-1.375	-0.05	-0.15	-0.18	-0.004
<b>Modified Configuration</b>	-1.375	-0.06	-0.25	-0.46	-0.005

Pitch angle time response



	$K_\alpha$	$K_q$	$K_P$	$K_I$	$K_D$
<b>Base Configuration</b>	-1.375	-0.05	-0.15	-0.18	-0.004
<b>Modified Configuration</b>	-1.375	-0.05	-0.15	-0.18	-0.004

Pitch angle time response



- ☐ Temporal response is faster with the modified configuration.
- ☐ Lower settling time and rise time.
- ☐ Dynamic response of the vehicle is improved.



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## 5.0 CONCLUSIONS

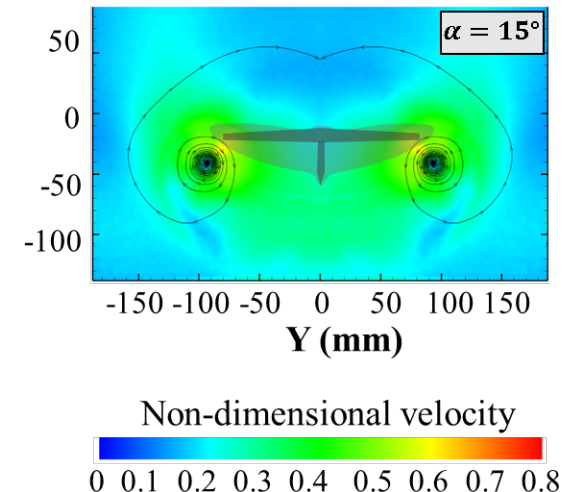
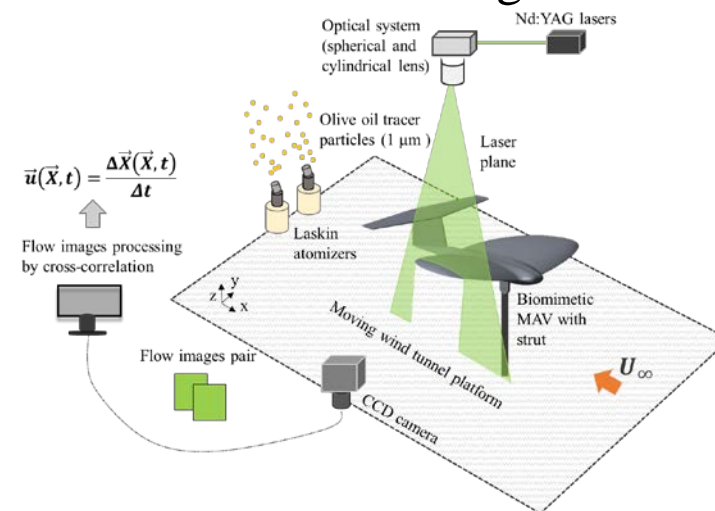
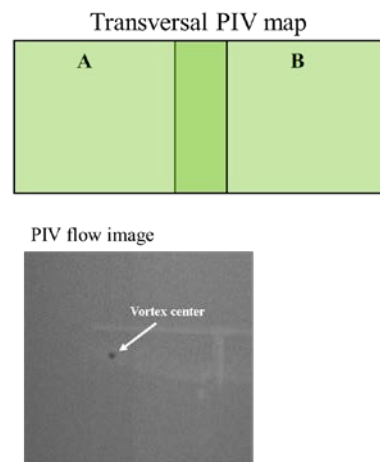
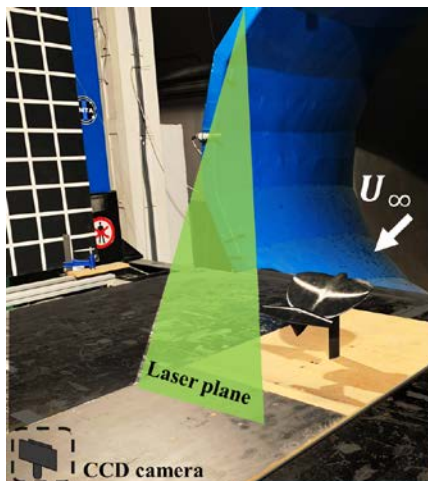
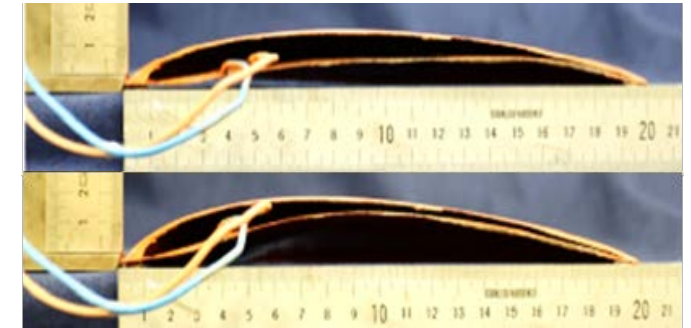
- ❑ The flight control system of the morphing base configuration has been redesigned for its modified configuration, obtaining **an increased static stability and improved dynamic response.**
- ❑ A strict minimum gain and phase margin requirements of 6 dB and 45° have been considered to conduct the redesign of the flight control system, together with a requirement of a maximum overshoot allowed of 20% of the stationary value.
- ❑ It has been demonstrated with the redesign that the slight stability improvement of the modified configuration can indeed lead to significant enhancements of the pitch angle dynamic time response if the autopilot gains are optimized.



## 5.0 CONCLUSIONS

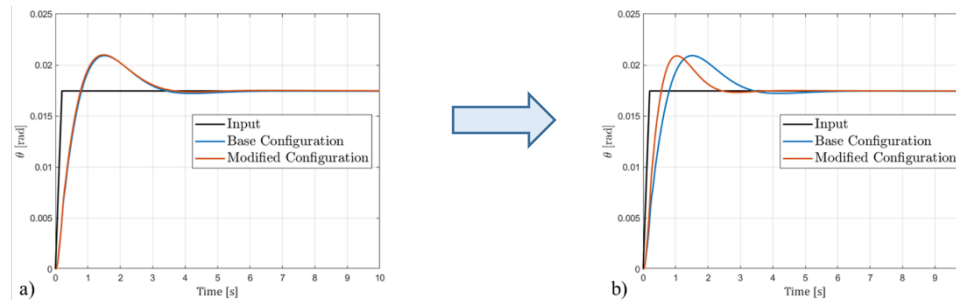
### Next steps:

- ✓ **1<sup>st</sup> phase:** Design of the morphing UAV.
- ✓ **2<sup>nd</sup> phase:** Ground testing – base and modified configurations.
- ✓ **3<sup>rd</sup> phase:** Aerodynamic characterization – wind tunnel testing and CFD simulation.



## 5.0 CONCLUSIONS

- 4<sup>th</sup> phase:** Longitudinal Stability of the base and modified UAV configurations.



- 5<sup>th</sup> phase:** Set dynamic gains that change with the applied voltage as the curvature changes.
- 6<sup>th</sup> phase:** Fabricate real demonstrator with Flight Test Instrumentation.
- 7<sup>th</sup> phase:** Flight Testing (pressure sensors, accelerometers and flight data recorders).

**THANK YOU FOR YOUR ATTENTION**

**QUESTIONS?**